

20710-214

TUTTOETS 11 / TUT TEST 11

2023

Voort's en Van / Init's and Surname:

MEMO

Studentenommer/ Student number:

Besluit of die kwadратiese kromme hieronder gegee 'n hiperbool of ellips is, en bereken dan die lengtes van die hoofasse en die rotasie-hoek. Maak dan 'n vryhand-skets waarop al die inligting aangedui is.

Decide whether the quadratic curve given below is a hyperbola or an ellipse, and then calculate the lengths of the semi-axes, and the rotation angle. Then draw a rough figure showing all the relevant information.

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$$7.4x^2 - 6.4xy + 2.6y^2 = 9$$

Wenk/Hint: $\mathbf{u}^T A \mathbf{u} = d$, $a = \sqrt{d/\lambda_1}$, $\sin \theta = -Q_{12}$

$$A = \begin{bmatrix} 7.4 & -3.2 \\ -3.2 & 2.6 \end{bmatrix} \quad \lambda_1 = 9 \quad \lambda_2 = 1$$

$$\lambda_1 = 9: \quad x^2 - 10x + 9 = 0, \quad \lambda_1 = 9, \quad \lambda_2 = 1$$

$$\lambda_2 = 1: \quad \begin{bmatrix} 6.4 & -3.2 \\ 0 & 0 \end{bmatrix} \begin{pmatrix} x_1 \\ \mu \end{pmatrix} = 0 \quad x_1 = \frac{1}{2}\mu$$

$$x_1 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$x_2 = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad Q = \frac{1}{\sqrt{5}} \begin{bmatrix} 2 & 1 \\ -1 & 2 \end{bmatrix} \quad L = \begin{bmatrix} 9 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\theta = -\arcsin\left(\frac{1}{\sqrt{5}}\right) = -26.57^\circ$$

$$a = \sqrt{\frac{9}{9}} = 1$$

$$b = \sqrt{\frac{9}{1}} = 3$$

