

20710-214	TUTTOETS 2 / TUT TEST 2	2023
Voorl's en Van / Init's and Surname:	MEMO	
Studentenommer / Student number:		

In vrae 1 en 2 is  $A, B, C$ , en  $X$  is  $(n \times n)$  matrikse, en  $I$  is die  $(n \times n)$ -eenheidsmatriks. Neem aan dat waar ookal 'n inverse van 'n matriks benodig word, dit wel bestaan.

In questions 1 and 2,  $A, B, C$ , and  $X$  are  $(n \times n)$  matrices, and  $I$  is the  $(n \times n)$  identity matrix. Assume that the inverse of a matrix exists, whenever it is needed.

1 Vereenvoudig die volgende uitdrukkings:

Simplify the following expressions:

(a)  $(B^T(A^T + I))^T - B$

(b)  $(B(CAB + CB)^{-1}C)^{-1}$

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(a)  $[B^T(A^T + I)]^T - B = (A^T + I)^T (B^T)^T - B$   
 $= (A + I)B - B = AB + B - B = AB$

(b)  $[B(CAB + CB)^{-1}C]^{-1} = C^{-1}(CAB + CB)B^{-1}$   
 $= C^{-1}CABB^{-1} + C^{-1}CBB^{-1} = A + I$

(a) AB ✓✓✓✓  
 (b) A+I ✓✓✓✓

2 Maak  $X$  die onderwerp van die formule in onderstaande vergelyking:

Make  $X$  the subject of the formula in the equation below:

$$(A + I)X = AB + X(I + B^{-1}A) - B^{-1}A$$

I apologize. This was completely unfair and too difficult. I have also not shown you any techniques in tackling this. This will not be graded. I apologize for the time you had to spend working on this.

$X = I + B$