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UNIVERSITY

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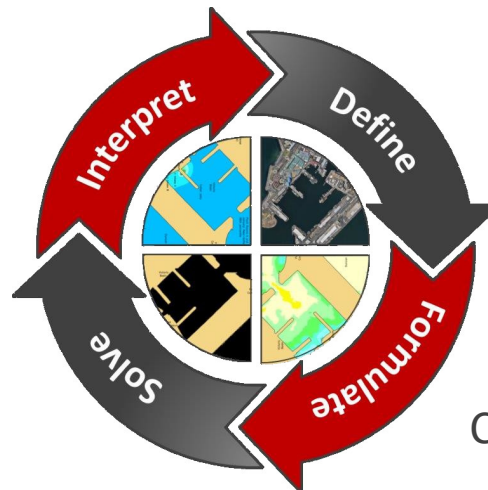
*forward together · saam vorentoe · masiye phambili*

# Postgraduate Opportunities

## Applied Mathematics

*The division of Applied Mathematics at Stellenbosch University focuses on research in numerical analysis and scientific computing, computer vision and machine learning, fluid dynamics and modelling, and applied discrete mathematics.*

*Our mission is to formulate and solve problems in all walks of life by making use of mathematical skills in an innovative way.*

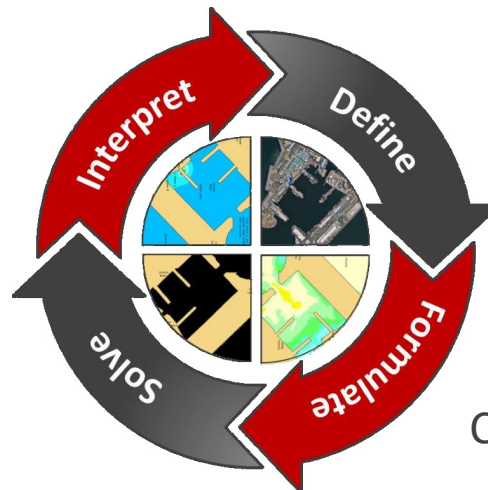


Contact: [appliedmaths@sun.ac.za](mailto:appliedmaths@sun.ac.za)

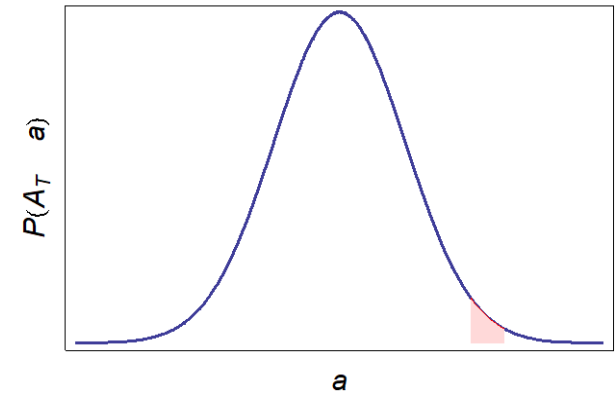
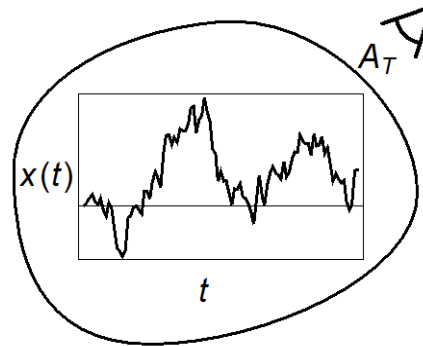
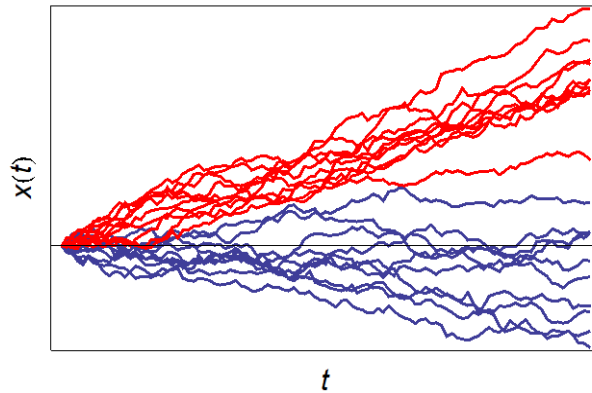
# Postgraduate Opportunities

- BSc Honours in Applied Mathematics
  - Prerequisites: 60% average for 3rd-year Applied Maths modules
- MSc in Applied Mathematics
  - Prerequisites: BSc Honours or B.Eng degree
- PhD in Applied Mathematics

## Research Projects

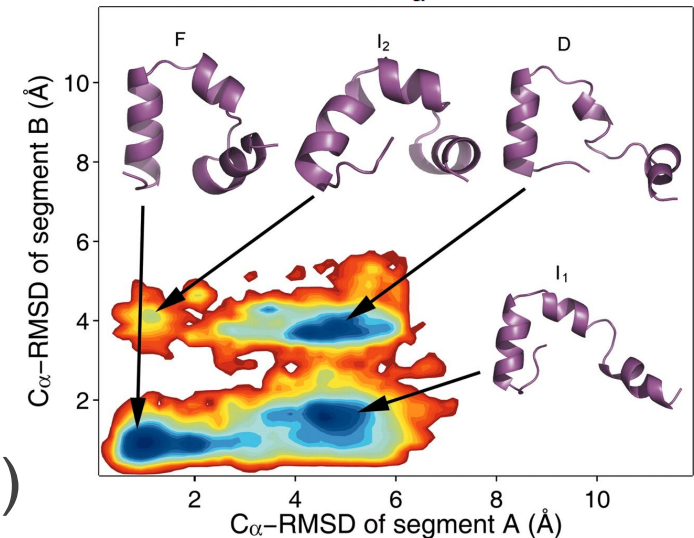


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## Topics

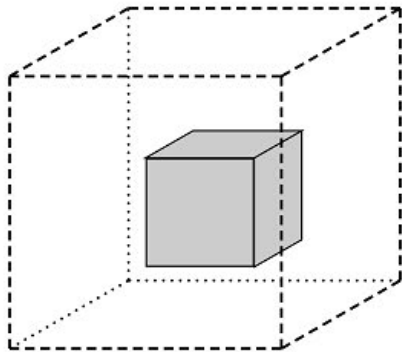
- Noisy systems (Markov processes)
- Estimation and prediction (learning)
- Simulations and sampling
- Rare transitions (crashes, change points)
- Physics applications



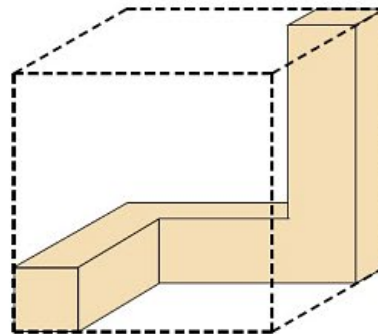
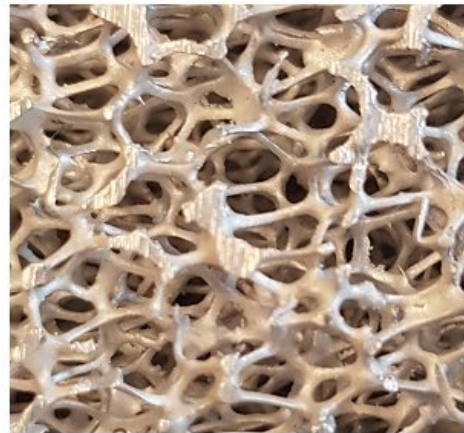


# Flow through Porous Media – Dr S Fidler

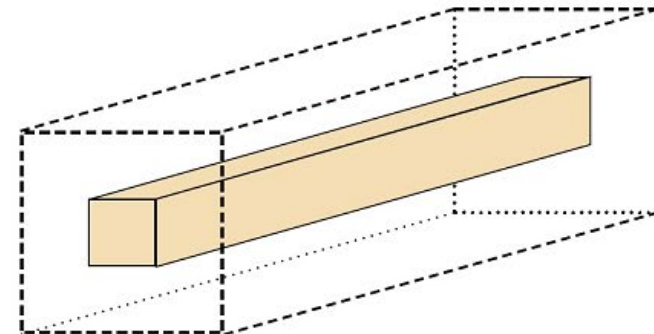
Granular Porous Medium



Metal Foam

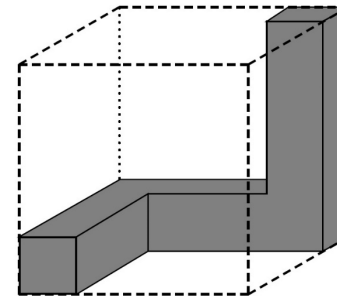
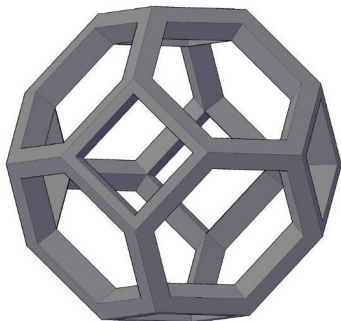
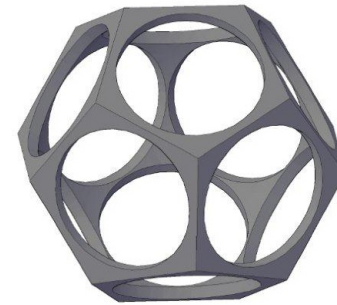
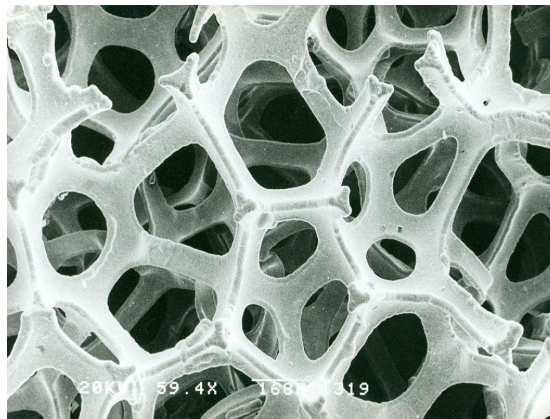
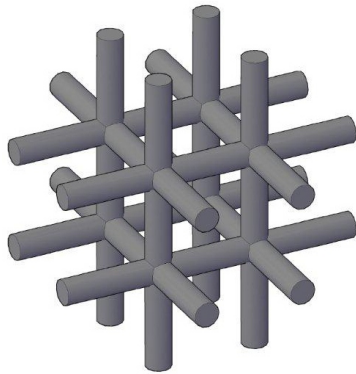


Fibrous medium

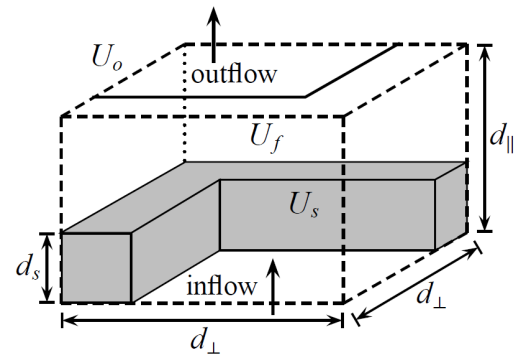
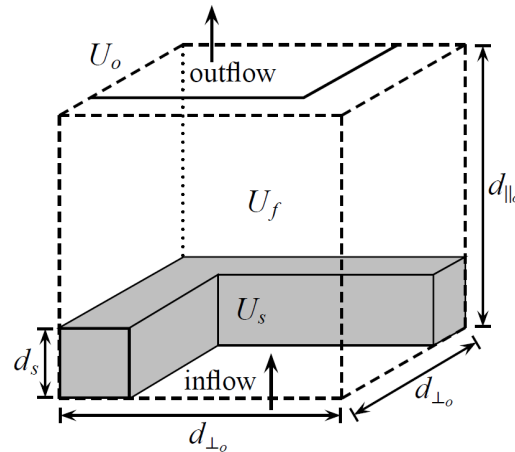
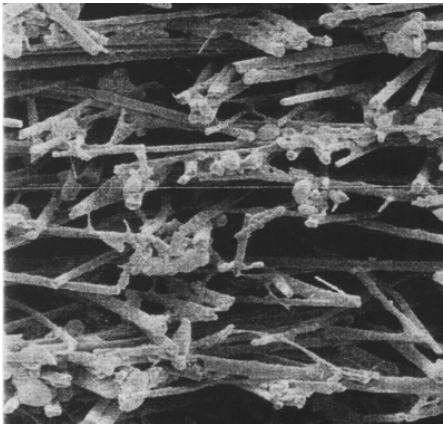
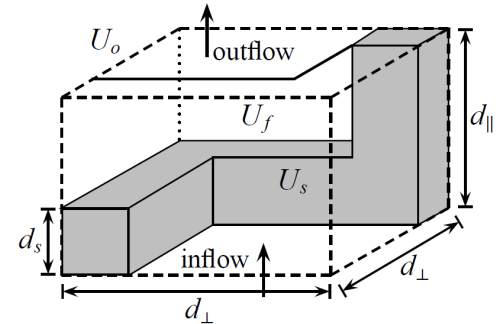
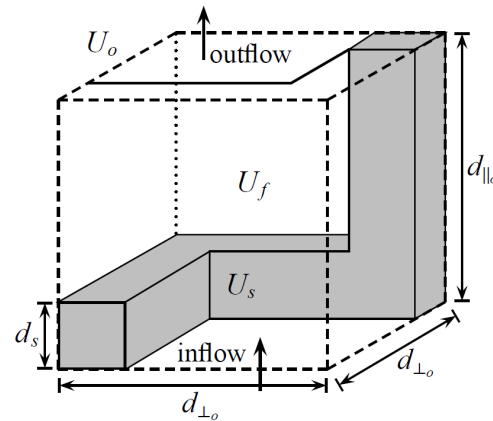
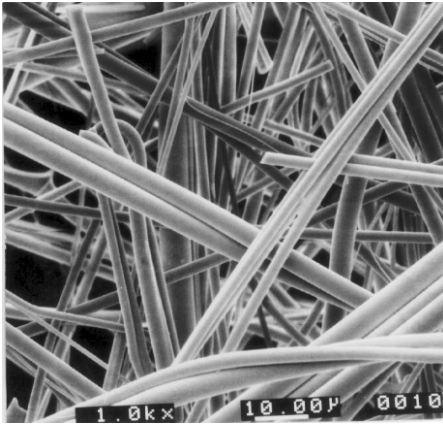


Geometric Models Representative of Average Medium Geometry

## Geometric models for metal foams



## AIR FILTRATION





## Sphericity

A diagram of a unit cell, represented by a dashed cube of side length  $d$ . Inside the unit cell is a smaller solid yellow cube of side length  $U_s$ . The unit cell is labeled  $U_o$  at the top-left corner. The fluid region within the unit cell is labeled  $U_f$ . A unit vector  $\hat{n}$  is shown pointing to the right. The side length  $d$  is indicated by arrows along the bottom and right edges of the unit cell.

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## Concluding remarks

### Advantages of our models

- Physically adaptable
- Based on sound physical principles – no empirical curve fitting parameters

### Outputs delivered from our models to date

- 15 MSc and PhD theses
- 40 journal papers

## Possible future work

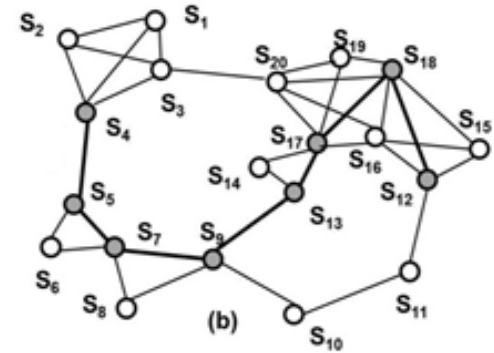
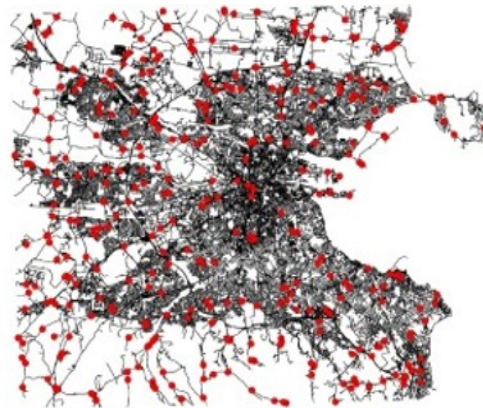
- Non-Newtonian flow combined with anisotropic geometry
- Taking particle size distributions into account
- Predict the formation factor in electrical conduction
- Accounting for the accumulation of solid material at the intersection of struts in the foam model
- Numerical flow simulations
- Etc.

# Graph theory – Riana Roux

## Domination in graphs

What are we modelling?

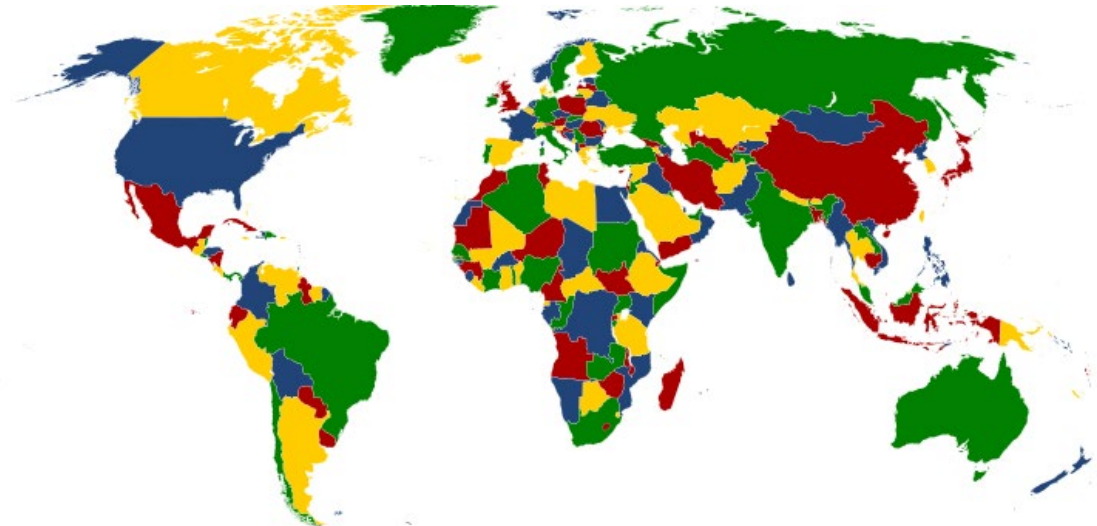
- Facility location problems
- Network protection



## Colouring a graph

What are we modelling?

- Scheduling
- Register allocation

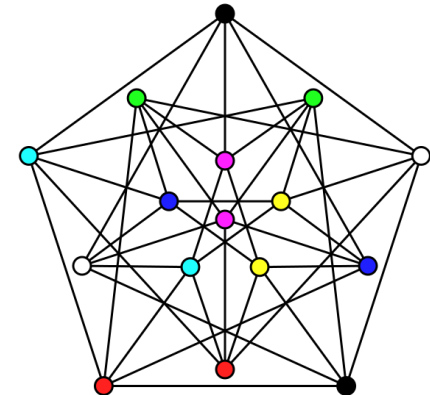
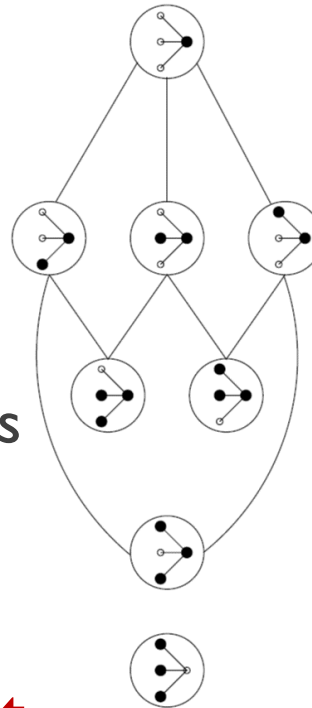




# Graph theory – Riana Roux

























































## Research topics

- Reconfiguration problems
- Effects of changes in a graph
- Complexity results
- Structural properties of graphs
- Games on graphs



## Graph parameters of interest

- Exponential and broadcast domination
- Equitable and consecutive colourings
- Ramsey colourings

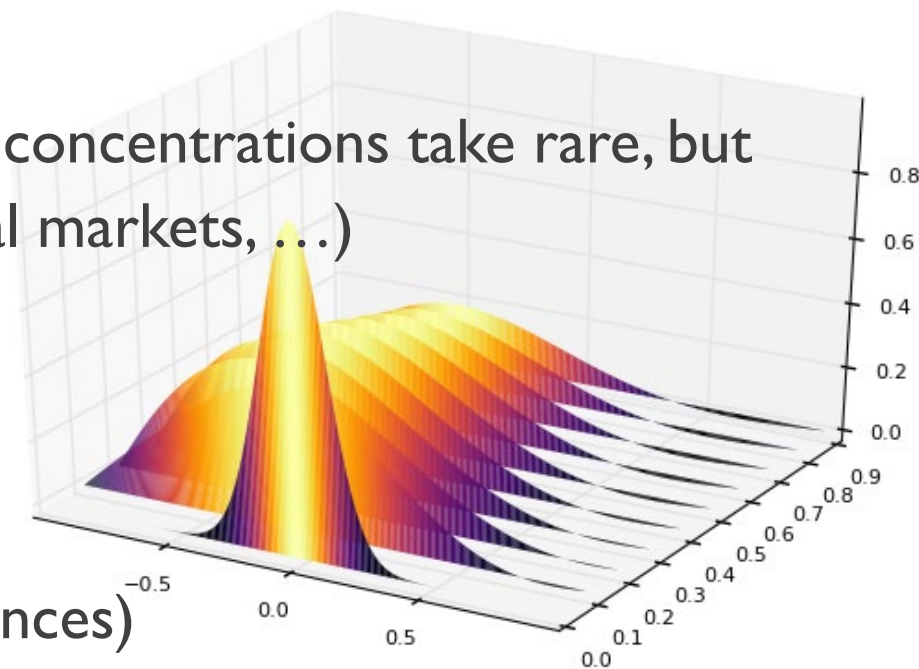
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## Fractional differential equations (FDEs)

FDEs are playing an ever-increasing role in the mathematical modelling of real-world phenomena.

“Super-diffusion”: processes where concentrations take rare, but large jumps (e.g., epidemics, financial markets, ...)

“Anomalous diffusion”: processes with a ‘memory’, (e.g., neural synapse responses and DNA sequences)



# Software for numerical solution of differential equations – Nick Hale

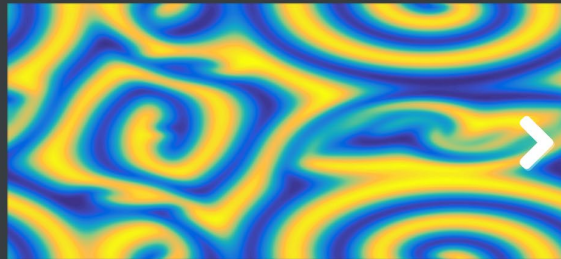
## Chebfun ([www.chebfun.org](http://www.chebfun.org))

- Well-written codes for numerical solution of DEs
- Automatic discretisation and grid refinement

### Applications:

- Numerical function approximation and optimisation
- ODEs and PDEs on rectangles, spheres, and disks
- ODE eigenvalue problems

```
% Create operator for Ginzburg-Landau problem
m
d = 20*[-1.2 3.2 -1 1];  tspan = [0 46.5];
S = spinop2(d,tspan); S.lin = @(u) lap(u);
S.nonlin = @(u) u - (1+1.5i)*u.*(abs(u).^2);
% Set initial condition, solve PDE, plot
S.init = chebfun2(@(x,y) ...
    (1i*x+y).*exp(-.03*(x.^2+y.^2)), d);
u = spin2(S, 128, 1e-1, 'plot', 'off');
plot(real(u))
```



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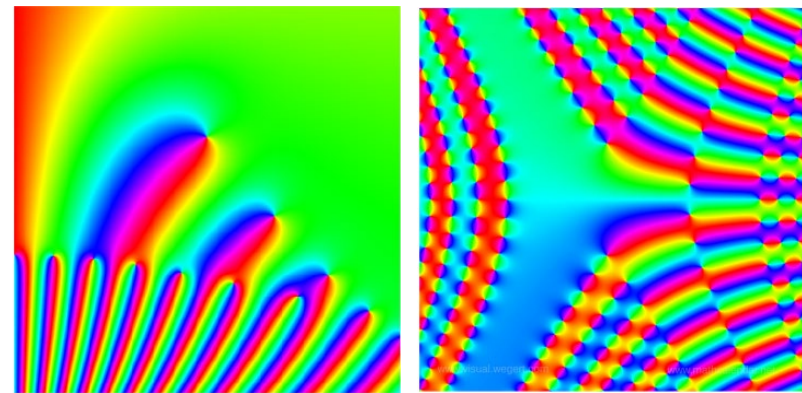


## Special functions

Certain special mathematical functions are ubiquitous in scientific and engineering investigations, e.g.,

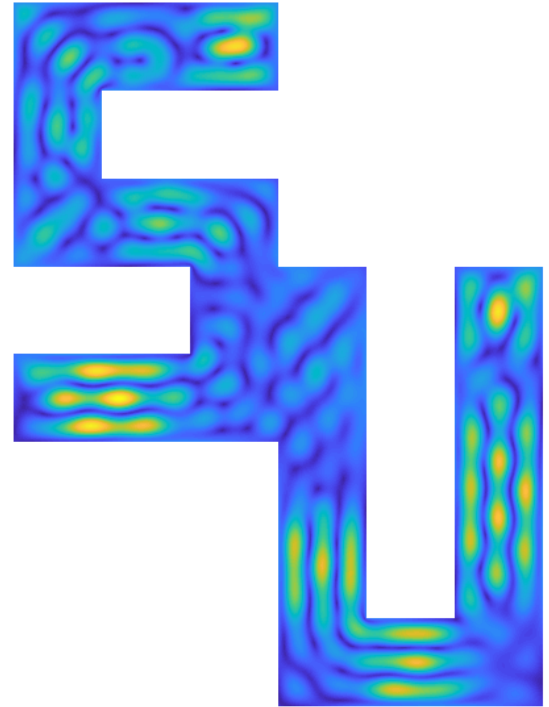
$$w(z) = \frac{i}{\pi} \int_{-\infty}^{\infty} \frac{e^{-t^2}}{z - t} dt, \quad u''(z) = 2u^3 + zu$$

- $w(z)$  is the plasma dispersion function, and occurs in astrophysics and spectroscopy.
- $u(z)$  is a Painleve function, and occurs in the computation of a certain probability distributions



## Other topics

- Spectral methods for ODEs and PDEs
- Fast large-scale numerical linear algebra
- Spectral deferred correction methods
- Radial basis function methods
- Function approximation
- Numerical complex analysis
- Computation of matrix functions
- Fast transforms and special functions



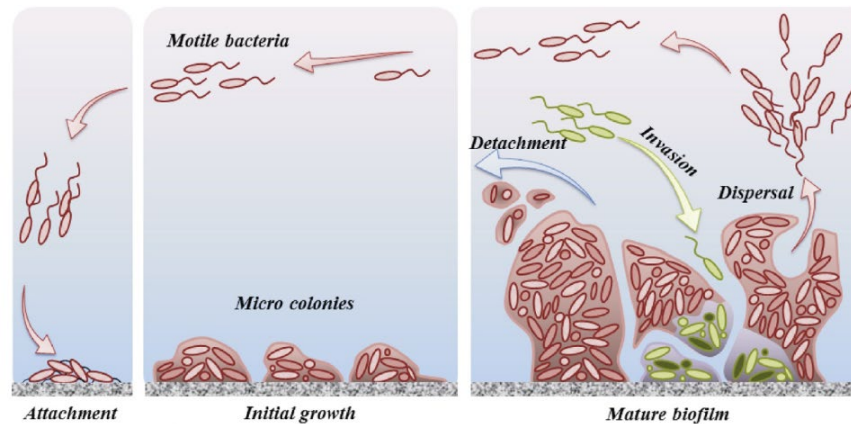
## Multiphysics, multiscale modelling

Fluid-Structure Interaction

Fluid mechanics

### Structure mechanics

- Viscoelastic
- Detachment?



D'acunto et al. (2019)

### Solving the equations:

- Finite Element Method
- High Performance Computing

### Growth modelling

Contact: [andiedevilliers@sun.ac.za](mailto:andiedevilliers@sun.ac.za)



# Modelling Biofilms— Andie de Villiers

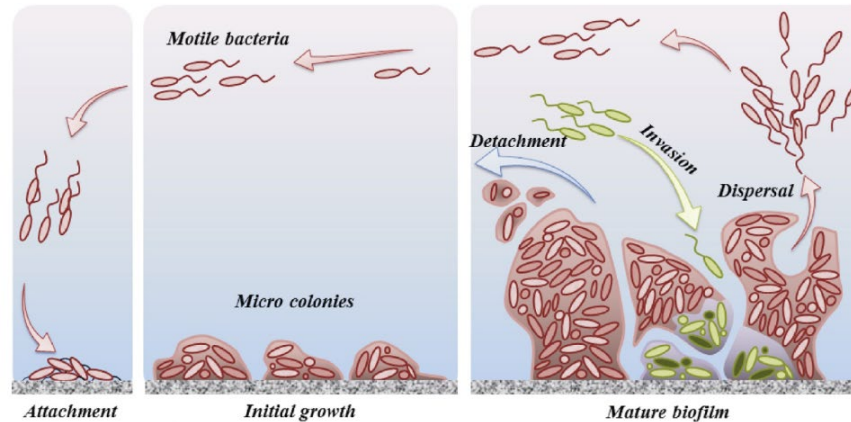
## Multiphysics, multiscale modelling

Fluid-Structure Interaction

Fluid mechanics

### Structure mechanics

- Viscoelastic
- Detachment?



D'acunto et al. (2019)

### Growth modelling

Solving the equations:

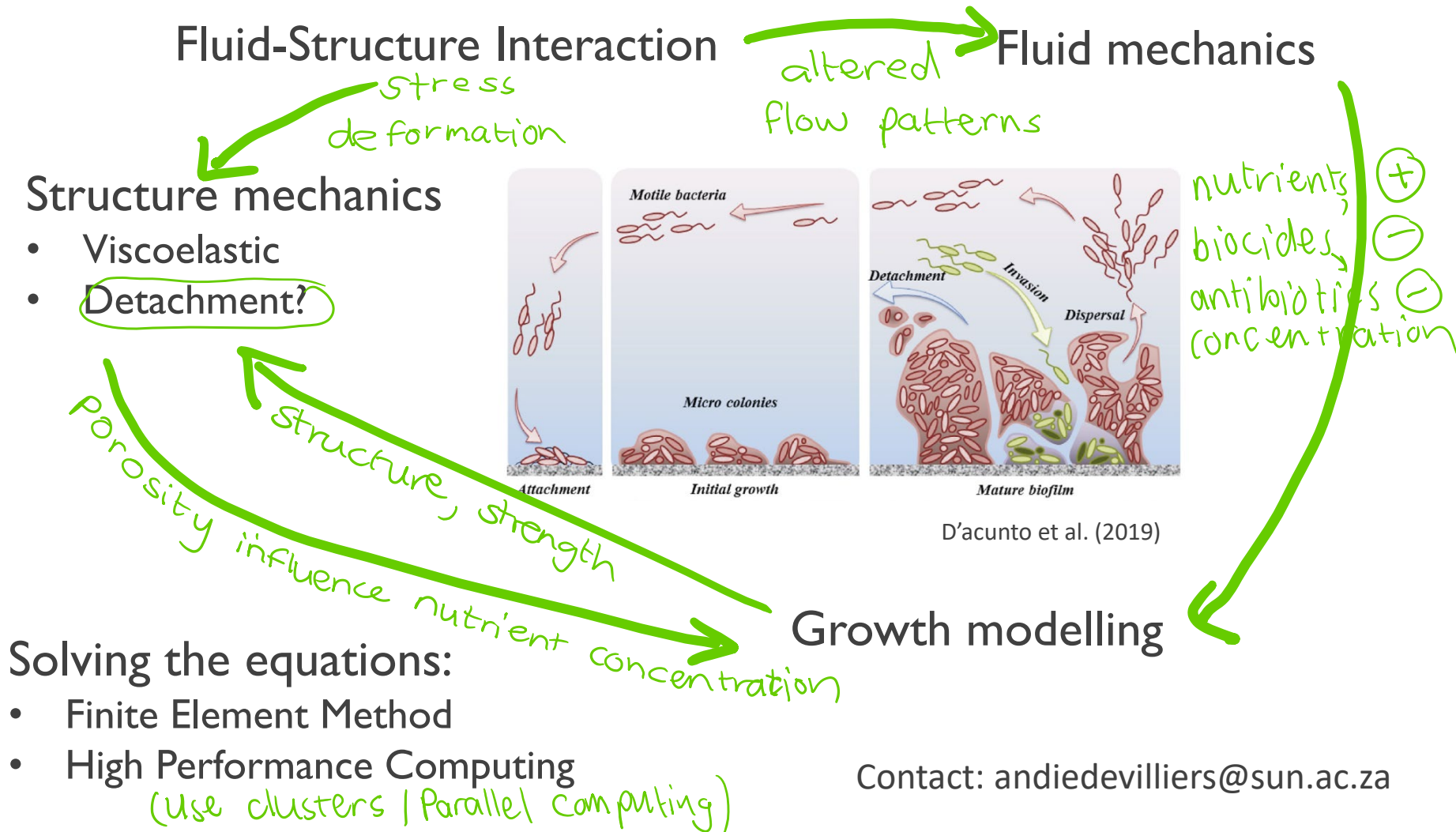
- Finite Element Method
- High Performance Computing

Contact: andiedevilliers@sun.ac.za

Continuum  
hydrodynamica  
time-scale

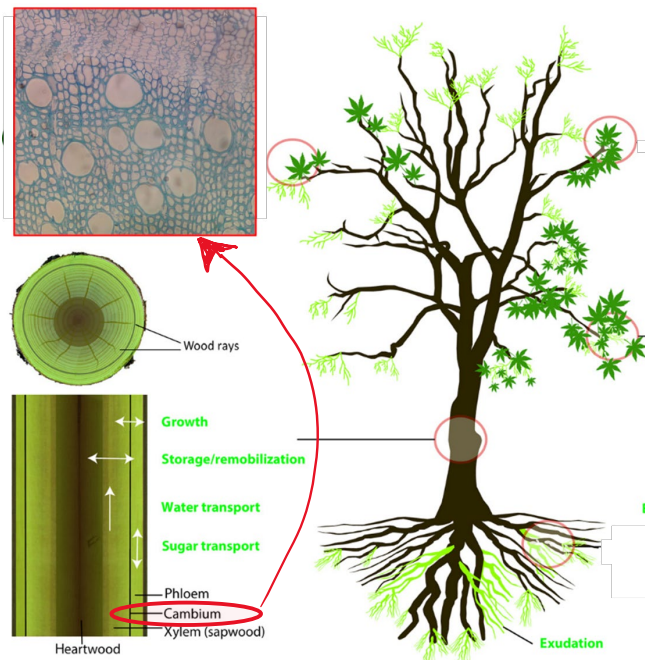
Micro scale  
(bacteria)  
longer  
timescale

## Multiphysics, multiscale modelling





## Funding Available for PhD and Masters students

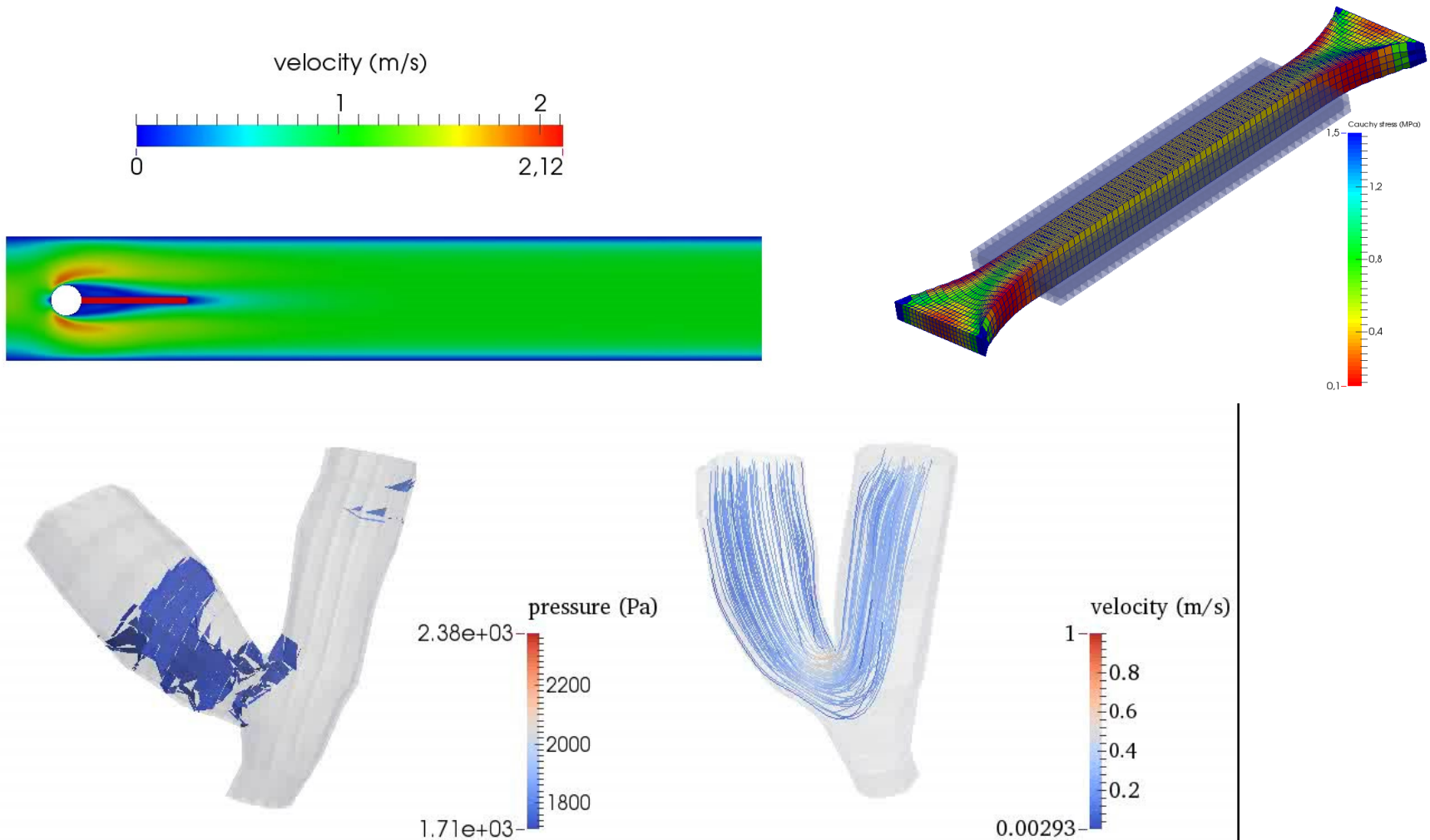


## Multiscale, Multiphysics modelling

- Plant-, tissue- and cell-level
- Cell mechanics
- Plant fluid mechanics
- Growth modelling

Contact: [drew@sun.ac.za](mailto:drew@sun.ac.za)  
[andiedevilliers@sun.a.za](mailto:andiedevilliers@sun.a.za)

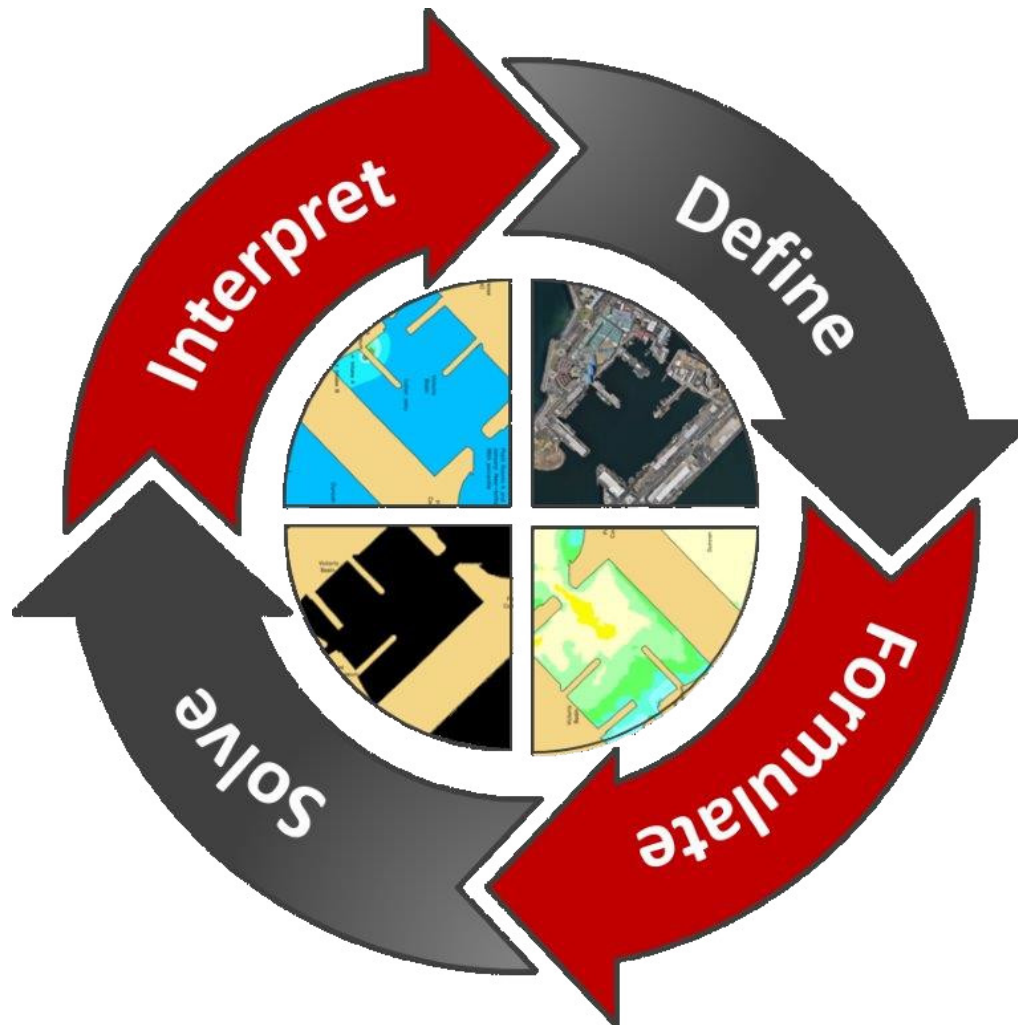
# Other topics - Andie de Villiers



Contact: [andiedevilliers@sun.ac.za](mailto:andiedevilliers@sun.ac.za)



# Questions?



Contact: [appliedmaths@sun.ac.za](mailto:appliedmaths@sun.ac.za)